## The KNAER Math Knowledge Network presents:

## Hour of Math + Code

## 4-10 December 2017 during Computer Science Education Week

In partnership with:


The Robertson Program
Inquiry-Based Teaching in $\begin{aligned} & \text { Mathematics and Science }\end{aligned}$


> BACK We are bringing back to the future TME FUTURE Coding for Young Mathematicians

## 1. Repeating Patterns

Go to researchideas.ca/patterns
Click on Example \#1. Click on Run This Code. Study the code and the result.


## Puzzle \#1

Edit the code to get this result:


## Puzzle \#2

Refresh your browser.
Edit the code to match changes circled at right.

Click on Run This Code to get this result.


Edit the code to get this result:

clear paths
new pattern
set size to 20
set stamp rate to 10

add blue ~ square ~ to pattern
repe/t 10 times
ro repeat 10 times


## Puzzle \#3

Edit the code to get this result:


## Puzzle \#4

Edit the code to get this result:


## Puzzle \#5

Edit the code to get this result:


## More?

Can't get enough of math + coding? Go to researchideas.ca/patterns
Get the PDF tutorials: on Repeating Patterns and Fractions

- Learn more ways to code repeating patterns.
- Learn to code fraction representations with repeating patterns.



## Making Challenges

Visit janettehughes.ca/lab/steam-challenges to investigate Making Challenges with repeating patterns!


## 2．Number Patterns

Numbers are beautiful．Especially on a grid．

| 1 | 2 | \％ | 4 | 5 | 940 | 7 | 8 | 940 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 969 | 13 | 14 | 8ai | 16 | 17 | （4） | 19 | 20 |
| 何 | 22 | 23 | 勺 | 25 | 26 | 绍 | 28 | 29 | （1） |
| 31 | 32 |  | 34 | 35 | 包 | 37 | 38 | ชิ | 40 |
| 41 | ช3 | 43 | 44 | M | 46 | 47 | Mo | 49 | 50 |
| \％ | 52 | 53 | \％ | 55 | 56 | ช8 | 58 | 59 | （1） |
| 61 | 62 | \％ | 64 | 65 | 閶 | 67 | 68 | （6） | 70 |
| 71 | －980 | 73 | 74 | 管碞 | 76 | 77 | 腬 | 79 | 80 |
| ชื | 82 | 83 | \％ | 85 | 86 | 录 | 88 | 89 | \％ |
| 91 | 92 | 诩 | 94 | 95 | $80$ | 97 | 98 | 993 | 100 |

Go to researchideas．ca／numbers
Click on Run Code．Study the code and the result．

| 1 | 2 | วอ | 4 | 5 | （6） | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 运 | 13 | 14 | ว่5 | 16 | 17 | ว⿶凵 | 19 | 20 |
| $\begin{array}{\|c\|} \hline 89 \\ \hline 80 \end{array}$ | 22 | 23 | $89$ | 25 | 26 | $829$ | 28 | 29 | 961 |
| 31 | 32 | \％aid | 34 | 35 | 840 | 37 | 38 | \％91 | 40 |
| 41 | $80$ | 43 | 44 | 90\％ | 46 | 47 | $8 \sqrt{96}$ | 49 | 50 |
| 8iai | 52 | 53 | $9 \mathrm{ai}$ | 55 | 56 | $8$ | 58 | 59 | \％） |
| 61 | 62 | \％aid | 64 | 65 | Biel | 67 | 68 | （6） | 70 |
| 71 | 8ais | 73 | 74 | $9$ | 76 | 77 | 8isi | 79 | 80 |
| 940 | 82 | 83 | 8is | 85 | 86 | 8aig | 88 | 89 | （9） |
| 91 | 92 | （2a） | 94 | 95 | 820 | 97 | 98 | （9） | 100 |



## Puzzle \#1

Click on Example \#1. Click on Run Code. Study the code and the result. Edit the code to get this result:

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 20\% | 16 | 17 | 18 | 19 | \%ai |
| 21 | 22 | 23 | 24 | 290 | 26 | 27 | 28 | 29 | \%ai |
| 31 | 32 | 33 | 34 | $8 \mathrm{~B}$ | 36 | 37 | 38 | 39 | (4) |
| 41 | 42 | 43 | 44 | $8$ | 46 | 47 | 48 | 49 | $81$ |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

## Puzzle \#2

Click on Example \#2. Click on Run Code. Study the code and the result. Edit the code to get this result:

| 1 | 2 | 3 | 4 | 5 | 6 | ง2\% | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | )48 | 15 | 16 | 17 | 18 | 19 | 20 |
|  | 22 | 23 | 24 | 25 | 26 | 27 | ब | 29 | 30 |
| 31 | 32 | 33 | 34 | 新 | 36 | 37 | 38 | 39 | 40 |
| 41 | A8 | 43 | 44 | 45 | 46 | 47 | 48 | 538 | 50 |
| 51 | 52 | 53 | 54 | 55 | अु | 57 | 58 | 59 | 60 |
| 61 | 62 | $3$ | 64 | 65 | 66 | 67 | 68 | 69 | \% |
| 71 | 72 | 73 | 74 | 75 | 76 | 960 | 78 | 79 | 80 |
| 81 | 82 | 83 | 99\% | 85 | 86 | 87 | 88 | 89 | 90 |
| 940 | 92 | 93 | 94 | 95 | 96 | 97 | 893⿺) | 99 | 100 |

## Puzzle \＃3

Click on Example \＃3．Click on Run Code．Study the code and the result． Edit the code to get this result：

| 1 | 2 | 8\% | 4 | 80 | $8$ | 7 | 8 | （20） | （\％） |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | $80$ | 13 | 14 | 205 | 16 | 17 | 263 | 19 | （4） |
| ais | 22 | 23 | 94i | क० | 26 | Rasi | 28 | 29 | （a） |
| 31 | 32 | $8$ | 34 | 8क－ | ?a | 37 | 38 | （9） | ） |
| 41 | $\begin{array}{r} 69 \\ 0 \\ 0 \end{array}$ | 43 | 44 | $5$ | 46 | 47 | 4－488） | 49 | P10 |
| अ98 | 52 | 53 | अ19 | （4） | 56 | （28） | 58 | 59 | （4） |
| 61 | 62 | （4） | 64 | （4） | जिए | 67 | 68 | ब18 | 网速 |
| 71 | 玲 | 73 | 74 | थि | 76 | 77 | คื่ | 79 |  |
| 钱 | 82 | 83 | अै | なiv | 86 | अ⿵冂 | 88 | 89 | 8 |
| 91 | 92 | ？ | 94 | Re | Ber | 97 | 98 | \％ | 12 |

## Puzzle \＃4

Click on Example \＃2．Click on Run Code．Study the code and the result． Edit the code to get this result：

| 1 | 2 | \％ | 4 | 5 | 4 | 7 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \％ | 10 | 11 | 6 | 13 | 14 | $\cdots$ | 4 |
| 17 | ข | 19 | 3 | ใ | 22 | 23 | 2 |
| 25 | 26 | 29 | 2 | 29 | ？${ }^{\text {a }}$ | 31 | ？35 |
| 3 | 34 | 35 | \％ | 37 | 38 | \％ | $\cdots$ |
| 41 | 9 | 43 | 9 | 265 | 46 | 47 | 2as |
| 49 | 50 | 震 | 2930 | 53 | 2aid | 55 | 2as |
| 80， | 58 | 59 | 9i9 | 61 | 62 | 903 | － |
| 65 | 28as | 67 | 20ia | 969 | 70 | 71 | 2ais |
| 73 | 74 | 963 | 80\％ | 77 | 9aid | 79 | （9） |
| 嘘 | 82 | 83 | 9aid | 85 | 86 | 963 | 9as） |
| 89 | （8） | 91 | 9 | \％ | 94 | 95 | 20 |

## More?

## MORE PUZZLES

Click on New Puzzle. Study the pattern of circled numbers. Can you create code that decorates the circled numbers differently from the rest?

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

## CREATE PUZZLES

Create your own puzzle. Then, save and share for others to solve. Here is some sample code.

## SAVE \& SHARE

Click on Save Code and name your project. The URL that appears under the Project Name can be shared.


## Making Challenges

Visit janettehughes.ca/lab/steam-challenges to investigate Making Challenges with number patterns!


## 3. Growing Patterns

In the story Anno's Magic Seeds, Jack has 2 magic seeds. Each seed will sustain him for 1 year. Each seed planted also produces 2 new seeds in one year.

In Year 1, Jack eats 1 seed and plants the other, to get 2 new seeds. In Year 2, Jack eats 1 seed and plants the other, to get 2 new seeds. He continues like this for a number of years.

Go to researchideas.ca/seeds


Click on Example \#1, and then on Run Code, to model this pattern.


## Puzzle \#1

What would happen if Jack finds something else to eat, and does not eat any of the seeds?

Would he have 10 seeds more at the end of the 10 years?

How could you edit the code to model this
 pattern?

## Puzzle \#2

In the story, eventually Jack decides to plant both seeds, and eat something else that year. The 2 seeds grow into 4 seeds. Next year, he eats 1 seed, and plants 3 , to get 6 seeds. He then eats 1 seed and plants 5 . How will his number of seeds grow if he continues in this way?

Click on Example \#2, and then on Run Code, to model this pattern.
Jack has a partner named Alice. Suppose they start with 2 seeds. How should Jack and Alice plan what they eat and plant?

Edit the code to model their plan.

## SAVE \& SHARE

Click on Save Code and name your project. The URL that appears under the Project Name can be shared.

## With Python

Go to cscircles.cemc.uwaterloo.ca/console
Enter the code below. Click on Run Program. Study the code and the output.
How is it similar to, or different from, the code that solves Puzzle 1?

```
    1 seeds = 2
    2 for year in range(1,11):
    3 if year == 1:
    \(4 \quad\) eaten \(=0\)
    5
    else:
        eaten = 1
    planted = seeds - eaten
    grown \(=\) planted * 2
    seeds \(=\) seeds + grown - eaten - planted
10 print (year, seeds)
```


## Making Challenges

Visit janettehughes.ca/lab/steam-challenges to investigate Making Challenges with growing patterns!


